

# Core–Shell-Structured Dielectric–Metal Circular Nanodisk Antenna: Gap Plasmon Assisted Magnetic Toroid-like Cavity Modes

Qiang Zhang,<sup>†</sup> Jun Jun Xiao,<sup>\*,†</sup> Xiao Ming Zhang,<sup>†</sup> Dezhuan Han,<sup>‡</sup> and Lei Gao<sup>§</sup>

<sup>†</sup>College of Electronic and Information Engineering, Shenzhen Graduate School, Harbin Institute of Technology, Shenzhen 518055, China

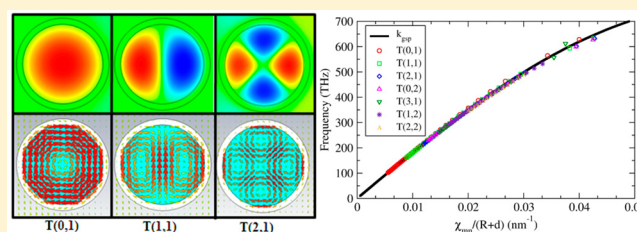
<sup>‡</sup>Department of Applied Physics, Chongqing University, Chongqing 400044, China

<sup>§</sup>Jiangsu Key Laboratory of Thin Films, School of Physical Science and Technology, Soochow University, Suzhou 215006, China

## S Supporting Information

**ABSTRACT:** Plasmonic nanoantennas, the properties of which are essentially determined by their resonance modes, are of interest both fundamentally and for various applications. Antennas with various shapes, geometries, and compositions have been demonstrated, each possessing unique properties and potential applications. Here, we propose the use of a sidewall coating as an additional degree of freedom to manipulate plasmonic gap cavity modes in strongly coupled metallic nanodisks. It is demonstrated that for a dielectric middle layer with a thickness of a few tens of nanometers and a sidewall plasmonic coating of more than ten nanometers, the usual optical magnetic resonance modes are eliminated, and only magnetic toroid-like modes are sustainable in the infrared and visible regime. All of these deep-subwavelength modes can be interpreted as an interference effect from the gap surface plasmon polaritons. Our results will be useful in nanoantenna design, high-Q cavity sensing, structured light-beam generation, and photon emission engineering.

**KEYWORDS:** plasmonics, nanoantenna, toroidal mode, optical magnetic resonance



Surface plasmon polaritons (SPPs) are known as the collective oscillations of conductive electrons at metallic nanostructures and their interfaces.<sup>1,2</sup> When the optical field couples with the SPPs in plasmonic nanostructures, some fascinating features and applications arise, such as strong local field enhancement,<sup>3–5</sup> imaging beyond the diffraction limit,<sup>6–10</sup> and extraordinary transmission through periodic arrays of subwavelength holes in optically thick metallic films.<sup>11,12</sup> Indeed, any plasmonic nanostructure can be regarded as an optical nanoantenna or plasmonic resonator because of its ability to radiate and collect light, similar to the behavior of RF antennas in the microwave regime.<sup>13–16</sup> Moreover, because of the deep-subwavelength localization and strong enhancement of the local fields, plasmonic antennas have attracted considerable attention for their promising potential applications in areas such as optoelectronic integrated circuits,<sup>17,18</sup> surface-enhanced Raman scattering detection,<sup>19–22</sup> plasmonic sensing,<sup>23–25</sup> optical micromanipulation,<sup>26,27</sup> and light harvesting.<sup>28–30</sup>

Recently, circular metal–dielectric–metal resonators (CMDMRs) have been studied as plasmonic microcavities for various applications because of their extremely high *Q* factor and low modal volume.<sup>31–38</sup> The field patterns of the resonance modes in a CMDMR are similar to the whispering gallery modes (WGMs) in a high-refractive-index dielectric disk. Therefore, these modes are known as WGM-like plasmonic cavity modes in the literature.<sup>34,35</sup> More notably,

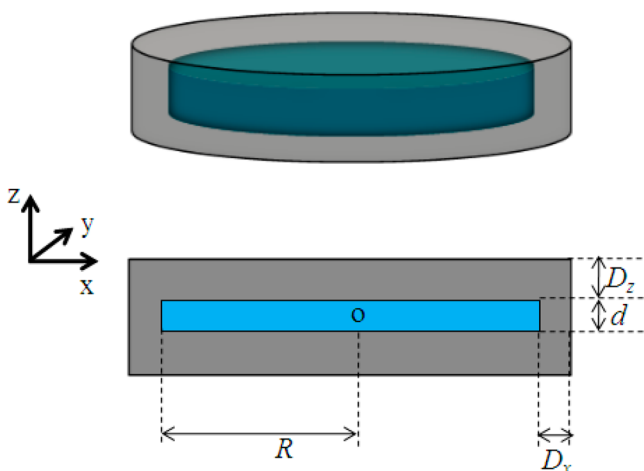
the in-plane magnetic field of one of the basic resonance modes in a CMDMR possesses a vortex distribution and has been interpreted as a predominant magnetic toroidal dipole.<sup>37,38</sup> This behavior is essentially enabled by the plasmon-resonance-induced displacement currents, which can overcome the saturation of the conduction current and promote the optical magnetic resonance from the terahertz up to the visible regime.<sup>39</sup> Filter et al. have established an analytical theory to explore the resonance properties of CMDMRs by defining a reflection coefficient of the gap SPPs at the termination of such a circular antenna.<sup>40</sup> It has been demonstrated that the optical field in the gap region of a CMDMR originates from the superimposed cylindrical gap SPPs. This type of coherent gap SPP is termed a Hankel-type or Bessel-type plasmonic standing wave.<sup>40,41</sup> The resonance modes in a CMDMR can be determined by solving the scalar Helmholtz equation in the structure with appropriate boundary conditions. At the lateral interface between the interior dielectric layer and the exterior air, the boundary condition is essentially the Neumann condition, e.g.,  $\partial E_z / \partial \rho = 0$ , where  $\rho$  is the radial component in cylindrical coordinates.<sup>36</sup>

In this work, we demonstrate that adding a sidewall metallic coating to a CMDMR can strongly affect the mode pattern and

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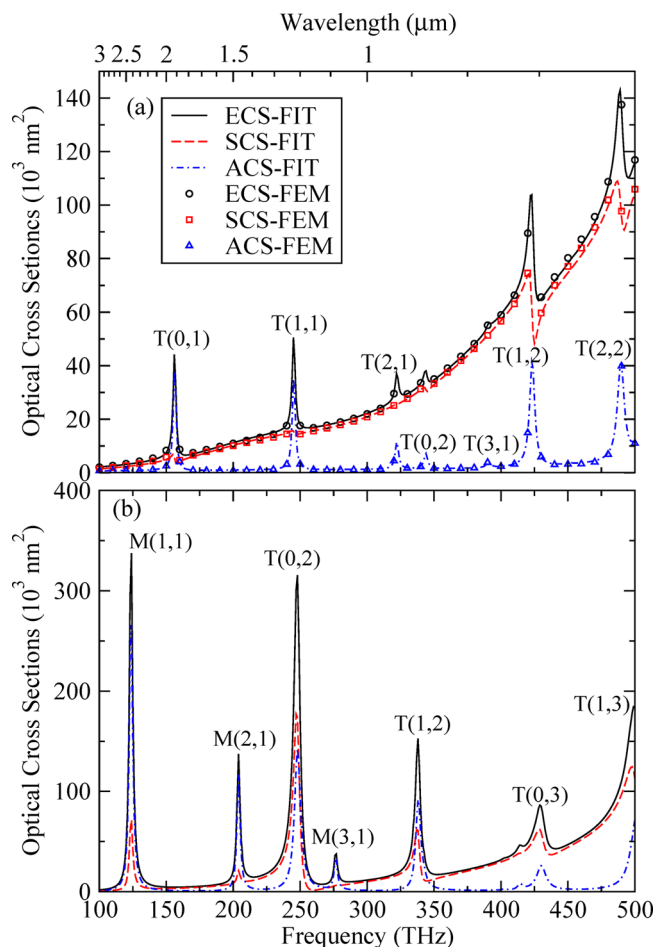
the optical characteristics of the cavity modes. Intuitively, the sidewall coating transforms the CMDMR from a sandwiched structure into a core-shell-structured nanodisk (CSND), representing a dramatic change (from an open cavity to a closed one) in geometrical topology (see Figure 1). The cavity



**Figure 1.** Schematic illustration of the geometry of the core-shell-structured nanodisk (CSND). A  $\text{SiO}_2$  nanodisk of radius  $R$  and thickness  $d$  is coated with silver layers. The thickness of the metallic layer in the  $z$  direction is  $D_z$ , and that in the  $x$  direction is  $D_x$ . The origin of the coordinate system is placed at the center of the  $\text{SiO}_2$  disk.

modes can be easily excited by an incident wave in a configuration that allows the magnetic component to cross the gap horizontally (see Section 1 of the Supporting Information for details). However, unlike the open cavity of a CMDMR, all cavity modes in a CSND have magnetic fields with vortex patterns. That is, the in-plane magnetic fields are purely combinations of magnetic vortices, making them similar to the hybridized modes of magnetic toroidal dipoles. We further demonstrate that all these toroid-like cavity modes follow the dispersion relation of the gap SPPs. The resonance condition is approximately given by the Dirichlet boundary condition  $E_z(\rho) = 0$  at the edge of the dielectric layer.

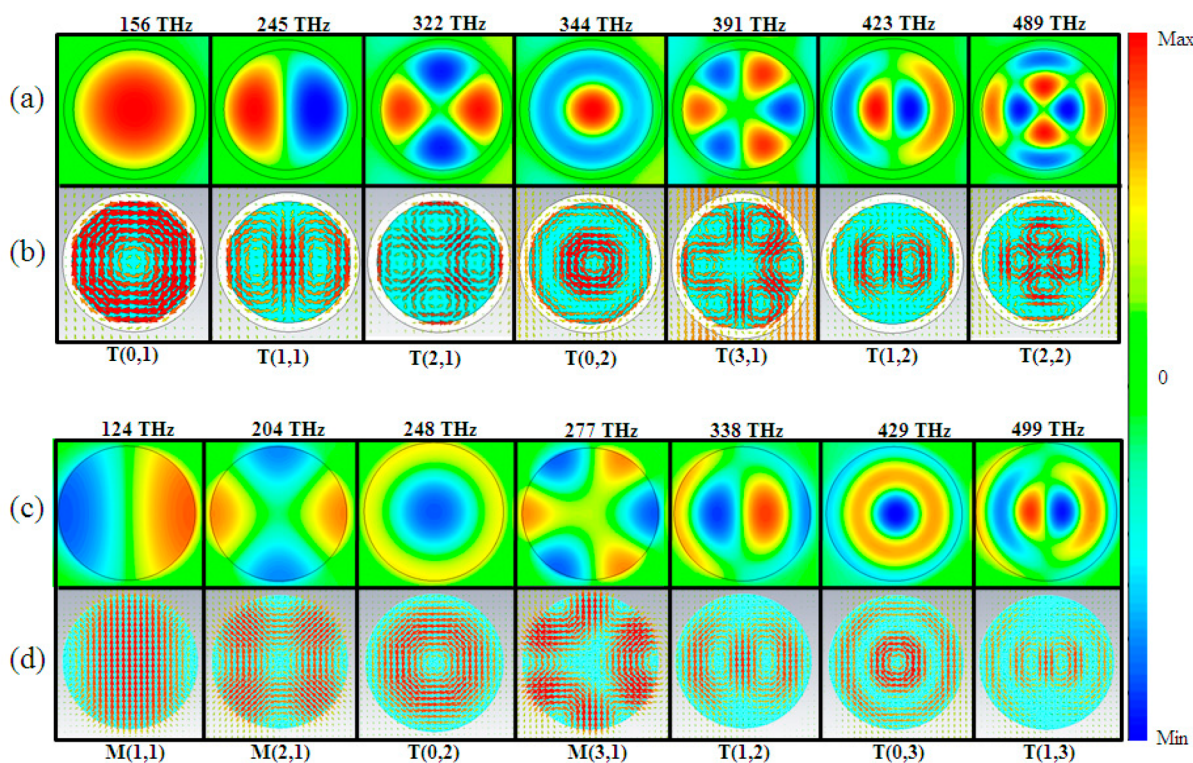
Figure 1 schematically illustrates the CSND, which consists of a concentric  $\text{SiO}_2$  circular disk and a silver coating. The permittivity of  $\text{SiO}_2$  is set to  $\epsilon_d = 2.1$ , and that of silver,  $\epsilon_m$ , is taken from Johnson and Christy.<sup>42</sup> To examine the cavity modes in the CSND, we consider a  $z$ -polarized plane wave propagating along the  $x$  direction that is incident upon the CSND. We employed two different methods—the finite integration technique (FIT) and the finite element method (FEM)—to calculate the optical cross sections.<sup>43,44</sup> The results are presented in Figure 2a for  $R = 260$  nm,  $d = 20$  nm,  $D_z = 35$  nm, and  $D_x = 40$  nm. In the frequency band of interest, seven significant peaks are observed in the absorption cross section (ACS; see the blue dash-dotted line). The frequencies of these peaks are  $f = 156$  THz ( $\lambda = 1923$  nm), 245 THz (1224 nm), 322 THz (932 nm), 344 THz (872 nm), 391 THz (767 nm), 423 THz (709 nm), and 489 THz (613 nm). These peaks are also observable in the extinction cross section (ECS) and the scattering cross section (SCS). For the other two wave-excitation configurations, the plasmonic electric multipole modes dominate the optical response, and these gap cavity modes are so nearly “dark” as to be unobservable (see Figures S1 and S2 in the Supporting Information).



**Figure 2.** (a) Optical cross sections of the CSND with  $R = 260$  nm,  $d = 20$  nm,  $D_x = 40$  nm, and  $D_z = 35$  nm calculated using two numerical methods (the lines represent the CST Microwave Studio results, and the symbols represent the COMSOL Multiphysics results). The T modes are labeled at the corresponding peaks of the spectrum. (b) Optical cross sections of a CMDMR with the same geometry for  $D_x = 0$  nm. The cavity modes are categorized into M and T modes based on their in-plane magnetic field characteristics.

To identify these cavity modes, we plot the  $z$  component of the electric field,  $E_z$ , and the in-plane magnetic field vector in the middle slice ( $z = 0$  nm) of the structure in Figure 3a and b, respectively. Figure 3b reveals that the magnetic fields of all these cavity modes have vortex distributions. For the first mode at  $f = 156$  THz, the magnetic field is confined in a circular form. This mode is, in fact, a typical magnetic toroidal dipole mode with a dominant toroidal moment in the  $z$  direction.<sup>37,38</sup> For the remaining higher-order cavity modes, the magnetic field can consist of several vortices arranged in different fashions. Therefore, we regard these resonance cavity modes as toroid-like modes and use ad-hoc terminology, labeling them T modes to differentiate them from conventional magnetic modes. One can distinguish these modes by their azimuthal and radial numbers in the  $E_z$  field patterns (see Figure 3a). For example, the azimuthal and radial numbers of the first mode are “0” and “1”, respectively. Thus, this mode can be labeled T(0,1). All seven cavity modes in Figure 2a are labeled in a similar manner.

To elucidate the effects of the sidewall plasmonic coating on the field distributions of the cavity modes, the results of the no-coating situation (open-cavity case), i.e., the results for a CMDMR with the same geometry and  $D_x = 0$ , are also



**Figure 3.** (a) Patterns of the electric fields  $E_z$  of the seven cavity modes of the CSND. (b) Magnetic field distributions of the corresponding modes of the CSND. (c) Field patterns  $E_z$  of the seven cavity modes of the CMDMR. (d) Magnetic field distributions of the corresponding modes of the CMDMR. The resonance frequency of each mode is indicated above the patterns, and their labels are provided below the patterns. The color bar is normalized to the full data range in each case.

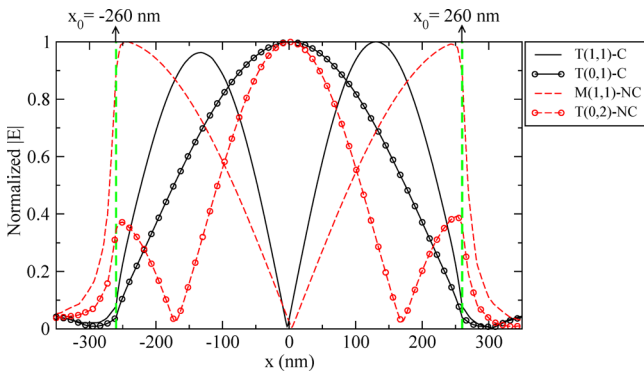
presented. The calculated optical spectra are presented in Figure 2b. Seven remarkable peaks are also observed in this case, at  $f = 124$  THz (2419 nm), 204 THz (1470 nm), 248 THz (1209 nm), 277 THz (1083 nm), 338 THz (887 nm), 429 THz (699 nm), and 499 THz (601 nm). The  $E_z$  and in-plane magnetic field patterns are presented in Figure 3c and d, respectively. Comparing Figure 3a and c, we observe that some of the cavity modes have nearly identical  $E_z$  distributions. For example, the pattern for  $f = 124$  THz in Figure 3c and that for  $f = 245$  THz in Figure 3a have the same azimuthal and radial numbers (1 and 1, respectively). However, the corresponding magnetic fields are quite different. The magnetic field at  $f = 124$  THz in Figure 3d and that at  $f = 245$  THz in Figure 3b are distinct: the latter exhibits a double-circle pattern, whereas the former exhibits a typical magnetic dipole distribution. On the basis of the magnetic field distributions depicted in Figure 3d, it is convenient to divide the cavity modes in the CMDMR into two categories. If the magnetic field of a mode does not form any vortices within the cavity, we can treat the field as a magnetic multipole (labeled with **M**). We regard the remaining modes as **T** modes, which also appear in the CSND case. On the basis of both the azimuthal and radial numbers represented in Figure 3c, all seven modes in the CMDMR can be labeled as  $\mathbf{M}(m,n)$  or  $\mathbf{T}(m,n)$ , as demonstrated in Figure 2b. It is important to note that none of the **M** modes survive when the sidewall plasmonic coating is present. This finding indicates that one of the effects of the sidewall coating is to eliminate the magnetic multipole cavity modes. Essentially, the **T**-mode and **M**-mode currents are different. The sidewall plasmonic coating prevents the conduction current from terminating on the upper or lower disk edge. Such edge termination of the current is crucial to the formation of **M** modes (see Figure S3 in the

Supporting Information). We replaced the silver of the sidewall coating with perfect electric conductor (PEC), and the results were nearly the same except for a small shift in the resonance frequencies (see Figure S4 in the Supporting Information). This finding strongly suggests that the sidewall provides a crucial bridge between the upper and lower disks for the induced current, which prevents the formation of the usual **M** modes in the CSND.

Another remarkable characteristic of the ECS (black solid lines) and SCS (red dashed lines) spectra shown in Figure 2a and b is that the resonance peaks of these cavity modes lie on the shoulder of a much broader resonance peak. We demonstrate that this broad resonance originates from the SPP resonance of the entire metallic shell by examining the near-field distribution and the current density at this frequency (see Figures S6 and S7 in the Supporting Information). The resonance occurs at much higher frequency ( $\sim 740$  THz), which is outside the range of Figure 2. This SPP exists at the interface between the metallic shell and the background (air). For convenience, we call this SPP an “exterior SPP” to distinguish it from the gap SPPs sustained in the dielectric core layer. Note that the upper and lower disk thicknesses are sufficiently large to disallow strong and direct evanescent wave coupling between the exterior SPP and the gap SPPs. However, the scattering interference between the exterior SPP mode and the relatively sharp gap SPP modes leads to an asymmetric spectrum, featuring a Fano profile (see Figure 2).

On the basis of the above results, we infer that the apparent differences in mode characteristics between the CSND and the CMDMR must result from the difference in the boundary condition in terms of the gap SPPs. To clarify this point, we examine the electric field at the edges of the dielectric layer.

Two corresponding pairs of modes in the CSND and CMDMR are selected as examples: one corresponding to T(1,1) in the CSND and M(1,1) in the CMDMR and the other corresponding to T(0,1) in the CSND and T(0,2) in the CMDMR. The two members of the former pair have the same azimuthal and radial numbers (1 and 1), whereas those of the latter pair have similar single-vortex magnetic fields (as observed in Figure 3b and c). For all four modes, the magnitude of  $E_z(x)$  along the  $x$  coordinate is shown in Figure 4.



**Figure 4.** Electric field along the radial direction, normalized to the corresponding maximum. The vertical green dashed lines indicate the edges of the SiO<sub>2</sub> at  $x_0 = \pm 260$  nm. The intersection points of the green dashed lines with the red dashed lines (for the CMDMR) are close to the local maxima, whereas those with the black solid lines (for the CSND) are close to zero.

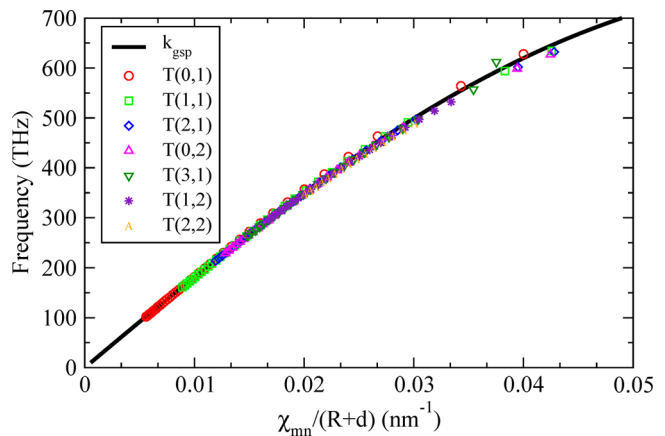
The two vertical dotted lines indicate the boundaries ( $\rho = R$ ) of the dielectric layer at  $x_0 = \pm 260$  nm. It is clearly observed that for the CMDMR the field  $E_z(x = x_0)$  is always close to its local maximum (dashed curves), whereas for the CSND,  $E_z(x = x_0)$  tends to be vanishing (solid curves). Moreover, if we use PEC as the material for the sidewall coating, then  $E_z(x = x_0)$  must be strictly equal to zero (see Figure S5 in the Supporting Information). For the noncoated case (the open cavity), the Neumann boundary condition  $\partial E_z(R)/\partial \rho = 0$  can be applied as an approximation, as reported in ref 36. In the meantime, we expect the Dirichlet boundary condition,  $E_z(R) = 0$ , to be appropriate in the coated case (the closed cavity).

In a circular patch nanoantenna, the solution to the Helmholtz equation for the  $z$  component of the electric field can be written in cylindrical coordinates:<sup>36</sup>

$$E_z(\rho, \phi, z) = a(z)[H_m^{(1)}(k_{\text{gsp}}\rho) + r_m H_m^{(2)}(k_{\text{gsp}}\rho)]e^{im\phi} \quad (1)$$

where  $m$  is an integer (angular quantum number),  $H_m^{(1,2)}$  is the  $m$ th Hankel function of the first or second type,  $k_{\text{gsp}}$  is the wave vector of the gap SPPs in the metal–dielectric–metal sandwich structure, and  $r_m$  represents the complex reflection coefficient of the Hankel-type SPP from the sidewall (lateral interface). In eq 1,  $a(z)$  is the evanescent modal profile in the  $z$  direction and  $\phi$  is the rotational angle. For the CMDMR, the Neumann boundary condition  $\partial E_z(R)/\partial \rho = 0$  is confirmed by plotting the resonance frequencies of the cavity modes versus  $\chi'_{mn}/(R + d)$ , where  $\chi'_{mn}$  represents the  $n$ th zero point of the derivative of the  $m$ th Bessel function  $J'_m(k_{\text{gsp}}\rho)$ .<sup>36</sup> In the CSND, the lateral boundary becomes a dielectric–metal interface, and the electric field nearly vanishes at  $\rho = R$  (see Figure 4). It is expected that the Dirichlet boundary condition  $E_z(\rho = R) = 0$  should approximately apply. We plot the resonance frequencies of the cavity modes in the CSND versus  $\chi_{mn}/R_{\text{eff}}$ ; here,  $\chi_{mn}$  is the  $n$ th

zero point of the  $m$ th Bessel function  $J_m(k_{\text{gsp}}\rho)$ . The effective radius can be approximated to first order as  $R_{\text{eff}} = R + d$ . As observed in Figure 5, the resonance points (symbols) of the



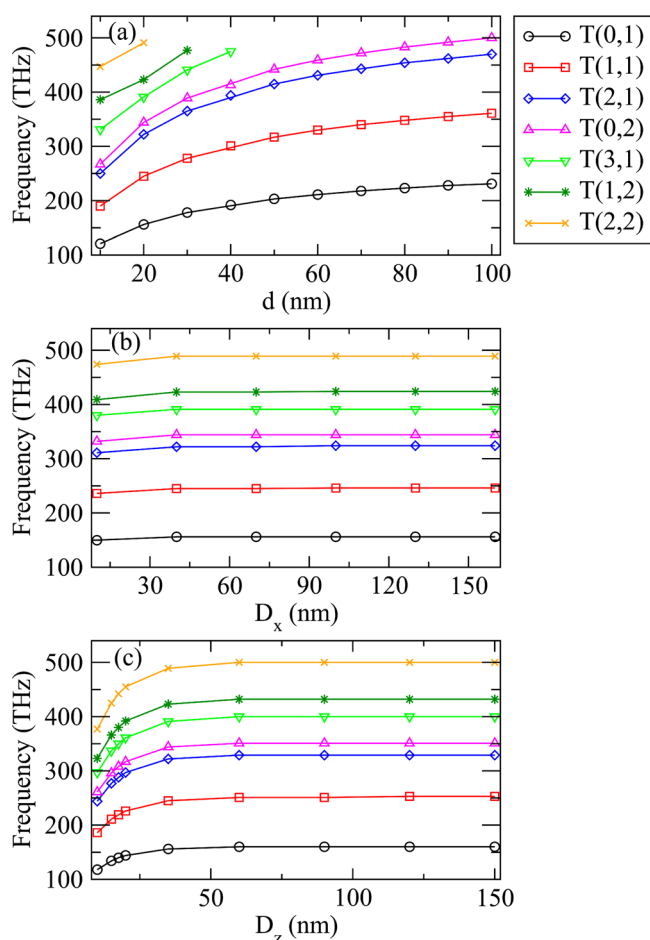
**Figure 5.** Resonance frequencies versus  $\chi_{mn}/(R + d)$ . The black solid line represents the dispersion relation of the gap SPPs obtained from eq 2.

considered seven toroid-like modes all fall on the curve of the dispersion relation (thick solid curve) of the gap SPPs,  $\omega(k_{\text{gsp}})$ . For simplicity, we assume that  $D_z \rightarrow \infty$  and  $k_{\text{gsp}}d \ll 1$ , yielding the following approximate expression for the dispersion relation of the gap SPPs:<sup>45,46</sup>

$$k_{\text{gsp}} \approx k_0 \sqrt{\epsilon_d + 0.5 \left( \frac{k_{\text{gsp}}^0}{k_0} \right)^2 + \sqrt{\left( \frac{k_{\text{gsp}}^0}{k_0} \right)^2 \left[ \epsilon_d - \epsilon_m + 0.25 \left( \frac{k_{\text{gsp}}^0}{k_0} \right)^2 \right]}} \quad (2)$$

In eq 2,  $k_0$  is the vacuum wave vector and  $k_{\text{gsp}}^0 = -2\epsilon_d/\epsilon_m$  is the wave vector of the gap SPPs in the limit of vanishing gap thickness ( $d \rightarrow 0$ ). The results presented in Figure 5 confirm that the gap surface plasmons with the lateral Dirichlet boundary condition are responsible for the emergence of the toroidal and toroid-like cavity modes. The ACS versus the disk size  $R$  in the frequency band from 100 to 500 THz, which quantifies the relative strength of the excitation, is plotted in Figure S8 in the Supporting Information.

Finally, the dependences of the resonance frequency on the geometric parameters  $d$ ,  $D_x$ , and  $D_z$  are in order. Figure 6a demonstrates that the resonance frequencies of all cavity toroid-like modes blue-shift as the gap thickness  $d$  increases. In fact, this blue-shift effect is also captured by the dispersion relation of the gap SPPs.<sup>46</sup> The dispersion curve governed by eq 2 and depicted in Figure 5 would ascend for increasing  $d$ . In an equivalent LC circuit model, a thicker dielectric layer results in smaller capacitance and causes the magnetic-field-induced antiparallel currents over the upper and lower disks to oscillate at a higher frequency. For the thickness  $D_x$  of the sidewall plasmonic coating, Figure 6b shows that the resonance frequencies remain nearly unchanged except in the case of a very thin metallic layer (e.g.,  $D_x < 20$  nm). This finding is observed because the electromagnetic field leaks laterally toward the exterior and interacts with the background field when the sidewall coating is not sufficiently thick. This leaky field effect could be utilized in sensing applications because the



**Figure 6.** Toroid-like mode resonance frequency versus (a) the thickness of the SiO<sub>2</sub> layer, (b) the thickness of the sidewall metallic coating, and (c) the thickness of the metallic layer in the *z* direction. The other parameters are the same as in Figure 2a, with only the indicated parameter varying in each panel.

cavity modes can be dramatically affected by outside perturbations near the CSND surface. The thickness  $D_z$  of the metallic layer in the *z* direction plays a key role in determining the effective refractive index of the gap SPPs, the dispersion relation, and the mode profile. Figure 6c demonstrates that the resonance frequencies are insensitive to  $D_z$  variations as long as  $D_z > 30$  nm, justifying the use of eq 2 in such cases. However, for  $D_z < 30$  nm, the dispersion relation represented by eq 2 deviates from the numerical data and must be replaced with a five-layer result in which the thickness of the metallic layer is finite and is appropriately considered.<sup>46</sup> Nevertheless, for larger  $D_z$ , the excitation efficiency of some cavity modes becomes too weak to observe (see Figure S9 in the Supporting Information). The small deviations observed in the high-frequency (high *k*-vector) regime of Figure 5 are partially attributable to the inaccuracy of eq 2 at small disk thicknesses, e.g.,  $D_z = 35$  nm in our case.

In a real application such as photoluminescence (PL) enhancement or spontaneous-emission control, a substrate must necessarily be present, and an active material covering (e.g., MEH-PPV) may be employed (see Figure S10 in the Supporting Information). In such a case, we demonstrate that it is possible to shift the exterior SPP frequency further away from those of the gap SPP modes because the substrate can substantially affect the exterior SPP. In the meantime, the gap

SPPs can remain intact. In particular, by virtue of field symmetry, it is demonstrated that for a dipole emitter located on the center axis of the cavity, the excitation of toroid modes with an azimuthal number of 0 becomes much stronger compared with the other modes (see Figures S11 and S12 in the Supporting Information). This effect provides a feasible approach to the exploration of the coupling dynamics between a quantum emitter and the magnetic toroidal moment by measuring the spectral and temporal PL spectra. The strain and conformation effects in the luminescent slab could also be interesting topics and require further exploration.

In conclusion, we theoretically and numerically investigated the resonance properties of the cavity modes in core–shell-structured dielectric–metal nanodisk antennas. The magnetic fields of all cavity modes in such resonators are observed to be dominated by vortex patterns, in either ring form or side-by-side form. Compared with the case of a conventional metal–dielectric–metal circular nanodisk antenna, we revealed that magnetic multipole cavity modes are eliminated by the core–shell structure. The plasmonic sidewall coating forces the electric fields at the lateral edge of the dielectric layer to nearly vanish and provides a bridge connecting the conduction currents in the upper and lower disks. All these deep-subwavelength cavity modes can be interpreted as a strong interference effect from the gap SPPs. The unique optical field distributions and the resonance properties in the CSND may be useful in exploiting toroidal metamaterials. Our results provide a new platform to explore the interactions of both fundamental and high-order toroidal modes and may find application in nanoantenna design, high-*Q* cavity sensing, structured light-beam generation, and photon emission engineering.

## ■ ASSOCIATED CONTENT

### 📄 Supporting Information

Responses for incident waves in the other two configurations; current density distributions in CSND and CMDMR; CSND with perfect electric conductor (PEC) sidewall coating; Fano effects from the interference between the exterior SPP and the gap SPP; absorption spectra for various dielectric disk radii; absorption spectra for various thicknesses of the metal layers; decay rates of an electric point dipole near the open and closed cavities. This material is available free of charge via the Internet at <http://pubs.acs.org>.

## ■ AUTHOR INFORMATION

### ✉ Corresponding Author

\*E-mail: [eiexiao@hitsz.edu.cn](mailto:eiexiao@hitsz.edu.cn).

### Notes

The authors declare no competing financial interest.

## ■ ACKNOWLEDGMENTS

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